

1b) $f(x) = x^2 - 2 - \cos x$ is continuous on $[0, \pi]$.

$f(0) = -3$ and $f(\pi) = \pi^2 - 1 \approx 8.87 > 0$. By the Intermediate Value Theorem, $f(c) = 0$ for at least one value of c between 0 and π .

2b) $g(t) = 2 \cos t - 3t$

g is continuous on $[0, 1]$.

$$g(0) = 2 > 0 \text{ and } g(1) \approx -1.9 < 0.$$

By the Intermediate Value Theorem, $g(c) = 0$ for at least one value of c between 0 and 1. Using a graphing utility to zoom in on the graph of $g(t)$, you find that $t \approx 0.56$. Using the root feature, you find that $t \approx 0.5636$.

3b) $f(x) = x^3 - x^2 + x - 2$

f is continuous on $[0, 3]$.

$$f(0) = -2 \text{ and } f(3) = 19$$

$$-2 < 4 < 19$$

The Intermediate Value Theorem applies.

$$x^3 - x^2 + x - 2 = 4$$

$$x^3 - x^2 + x - 6 = 0$$

$$(x - 2)(x^2 + x + 3) = 0$$

$$x = 2$$

($x^2 + x + 3$ has no real solution.)

$$c = 2$$

So, $f(2) = 4$.