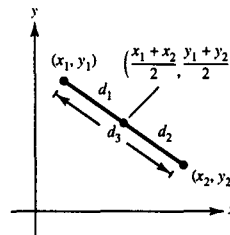


62. To show that  $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$  is the midpoint of the line segment joining  $(x_1, y_1)$  and  $(x_2, y_2)$  we must show that  $d_1 = d_2$  and  $d_1 + d_2 = d_3$  (see graph).

$$\begin{aligned} d_1 &= \sqrt{\left(\frac{x_1 + x_2}{2} - x_1\right)^2 + \left(\frac{y_1 + y_2}{2} - y_1\right)^2} \\ &= \sqrt{\left(\frac{x_2 - x_1}{2}\right)^2 + \left(\frac{y_2 - y_1}{2}\right)^2} = \frac{1}{2}\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ d_2 &= \sqrt{\left(x_2 - \frac{x_1 + x_2}{2}\right)^2 + \left(y_2 - \frac{y_1 + y_2}{2}\right)^2} \\ &= \sqrt{\left(\frac{x_2 - x_1}{2}\right)^2 + \left(\frac{y_2 - y_1}{2}\right)^2} = \frac{1}{2}\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ d_3 &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \end{aligned}$$

Therefore,  $d_1 = d_2$  and  $d_1 + d_2 = d_3$ .



### Appendix A.3

1. (a)  $396^\circ, -324^\circ$

(b)  $240^\circ, -480^\circ$

2. (a)  $660^\circ, -60^\circ$

(b)  $300^\circ, -60^\circ$

3. (a)  $\frac{19\pi}{9}, -\frac{17\pi}{9}$

(b)  $\frac{10\pi}{3}, -\frac{2\pi}{3}$

4. (a)  $\frac{7\pi}{4}, -\frac{\pi}{4}$

(b)  $\frac{26\pi}{9}, -\frac{10\pi}{9}$

5. (a)  $30\left(\frac{\pi}{180}\right) = \frac{\pi}{6} \approx 0.524$

(b)  $150\left(\frac{\pi}{180}\right) = \frac{5\pi}{6} \approx 2.618$

(c)  $315\left(\frac{\pi}{180}\right) = \frac{7\pi}{4} \approx 5.498$

(d)  $120\left(\frac{\pi}{180}\right) = \frac{2\pi}{3} \approx 2.094$

6. (a)  $-20\left(\frac{\pi}{180}\right) = -\frac{\pi}{9} \approx -0.349$

(b)  $-240\left(\frac{\pi}{180}\right) = -\frac{4\pi}{3} \approx -4.189$

(c)  $-270\left(\frac{\pi}{180}\right) = -\frac{3\pi}{2} \approx -4.712$

(d)  $144\left(\frac{\pi}{180}\right) = \frac{4\pi}{5} \approx 2.513$

7. (a)  $\frac{3\pi}{2}\left(\frac{180}{\pi}\right) = 270^\circ$

(b)  $\frac{7\pi}{6}\left(\frac{180}{\pi}\right) = 210^\circ$

(c)  $-\frac{7\pi}{12}\left(\frac{180}{\pi}\right) = -105^\circ$

(d)  $-2.637\left(\frac{180}{\pi}\right) \approx -135.6^\circ$

8. (a)  $\frac{7\pi}{3}\left(\frac{180}{\pi}\right) = 420^\circ$

(b)  $-\frac{11}{30}\left(\frac{180}{\pi}\right) = -66^\circ$

(c)  $\frac{11\pi}{6}\left(\frac{180}{\pi}\right) = 330^\circ$

(d)  $0.438\left(\frac{180}{\pi}\right) \approx 25.1^\circ$

9.

$r$	8 ft	15 in.	85 cm	24 in.	$\frac{12963}{\pi}$ mi.
$s$	12 ft.	24 in.	$63.72\pi$	96 in.	8642 mi.
$\theta$	1.5	1.6	$\frac{3\pi}{4}$	4	$\frac{2\pi}{3}$

10. (a)  $50 \text{ mph} = \frac{50(5280)}{60} = 4400 \text{ ft/min}$

Circumference of tire:  $C = 2.5\pi$  feet

Revolutions per minute:  $\frac{4400}{2.5\pi} \approx 560.2$

(b)  $\theta = \frac{4400}{2.5\pi}(2\pi) = 3520$  radians

Angular speed:  $\frac{\theta}{t} = \frac{3520 \text{ radians}}{1 \text{ minute}} = 3520 \text{ rad/min}$