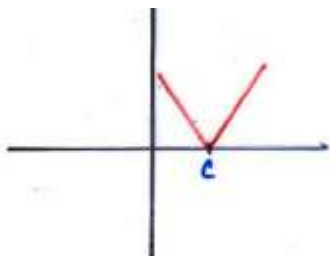


Differentiability

w-up: Graph $y = x^{2/3}$

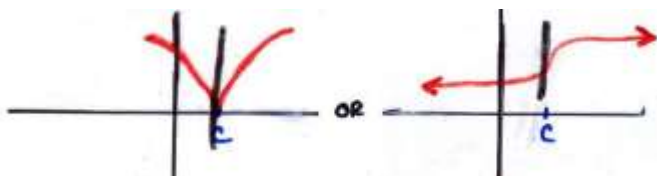
When derivatives CANNOT be found

- 1) Tangent lines have different slopes from the left and right at that x-value



Not differentiable at $x = c$

- 2) Tangent line vertical at that x-value (undefined slope)

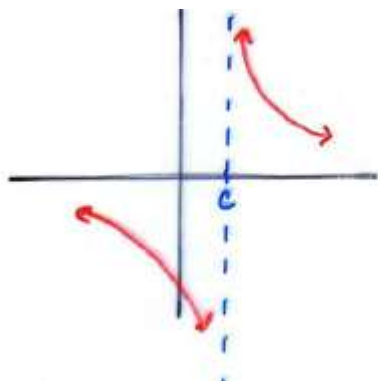


Not differentiable at $x = c$

Called a "cusp"

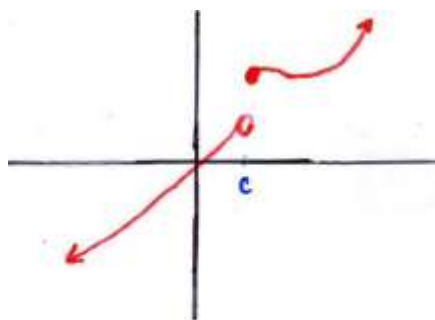
So..... Continuity does **not** necessarily mean Differentiability

- 3) Function undefined at that x-value



Not differentiable at $x = c$

4) Function is discontinuous at that x-value



Not differentiable at $x = c$

Write an example of function which models each of the four methods where derivatives cannot be found.

Derivatives of Piece-wise Functions

Determine intervals of differentiability for each function.

$$\text{A) } f(x) = \begin{cases} 2x - 2, & x < 2 \\ \frac{1}{2}x^2, & x \geq 2 \end{cases}$$

$$\text{B) } f(x) = \begin{cases} 3x^2 - 2, & x < 0 \\ 2x - 2, & x \geq 0 \end{cases}$$

For a piece-wise function to be differentiable everywhere, the graph must first be continuous at the x -value for the split domain (limit from left = limit from right.) Secondly, the derivative must also be the same at this x -value (slope from the left = slope from the right.)