

$$\begin{aligned}
 \text{1a)} \quad & \lim_{x \rightarrow -3} (x^2 + 3x) \\
 &= (-3)^2 + 3(-3) \\
 &= 9 - 9 = 0
 \end{aligned}$$

$$\text{1b)} \quad \lim_{x \rightarrow -4} (x + 3)^2$$

$$\text{1c)} \quad \lim_{x \rightarrow 7} \frac{3x}{\sqrt{x+2}}$$

$$\text{2a)} \quad \lim_{x \rightarrow 2} \frac{x^3 - 8}{x - 2}$$

$$\text{2b)} \quad \lim_{x \rightarrow -3} \frac{x^2 + x - 6}{x^2 - 9}$$

$$\text{2c)} \quad \lim_{x \rightarrow \pi/4} \frac{1 - \tan x}{\sin x - \cos x}$$

$$= \lim_{x \rightarrow 2} \frac{(x-2)(x^2 + 2x + 4)}{x-2}$$

$$= \lim_{x \rightarrow 2} (x^2 + 2x + 4)$$

$$= ((2)^2 + 2 \cdot (2) + 4)$$

$$= 12$$

$$\text{3a)} \quad \lim_{x \rightarrow 0} \frac{\sqrt{x+5} - \sqrt{5}}{x}$$

$$\text{3b)} \quad \lim_{x \rightarrow 4} \frac{\sqrt{x+5} - 3}{x-4}$$

$$= \lim_{x \rightarrow 0} \frac{\sqrt{x+5} - \sqrt{5}}{x} \cdot \frac{\sqrt{x+5} + \sqrt{5}}{\sqrt{x+5} + \sqrt{5}}$$

$$= \lim_{x \rightarrow 0} \frac{(x+5) - 5}{x(\sqrt{x+5} + \sqrt{5})}$$

$$= \lim_{x \rightarrow 0} \frac{1}{\sqrt{x+5} + \sqrt{5}}$$

$$= \frac{1}{2\sqrt{5}} = \frac{\sqrt{5}}{10}$$

$$\begin{aligned}
 \text{4a)} \quad & \lim_{x \rightarrow 0} \frac{[1/(3+x)] - (1/3)}{x} \\
 &= \lim_{x \rightarrow 0} \frac{\frac{1}{3+x} - \frac{1}{3}}{x} \\
 &= \lim_{x \rightarrow 0} \frac{3 - (3+x)}{(3+x)3(x)} \\
 &= \lim_{x \rightarrow 0} \frac{-x}{(3+x)(3)(x)} \\
 &= \lim_{x \rightarrow 0} \frac{-1}{(3+x)3} = -\frac{1}{9}
 \end{aligned}$$

$$\text{4b)} \quad \lim_{x \rightarrow 0} \frac{[1/(2+x)] - (1/2)}{x}$$

$$\begin{aligned}
 \text{5a)} \quad & \lim_{\Delta x \rightarrow 0} \frac{2(x + \Delta x) - 2x}{\Delta x} \\
 &= \lim_{\Delta x \rightarrow 0} \frac{2x + 2\Delta x - 2x}{\Delta x} \\
 &= \lim_{\Delta x \rightarrow 0} 2 = 2
 \end{aligned}$$

$$\text{5b)} \quad \lim_{\Delta x \rightarrow 0} \frac{(x + \Delta x)^2 - 2(x + \Delta x) + 1 - (x^2 - 2x + 1)}{\Delta x}$$

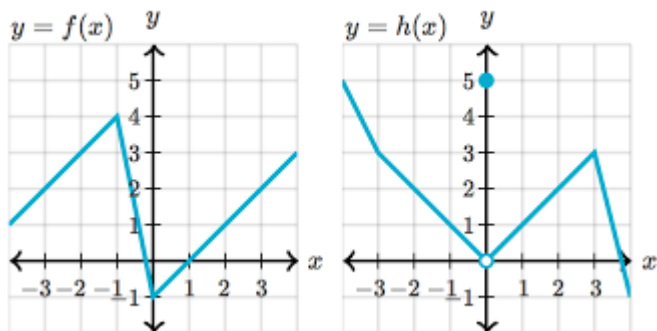
$$\begin{aligned}
 \text{6a)} \quad & \lim_{x \rightarrow 1} \cos \frac{\pi x}{3} \\
 &= \cos \frac{\pi}{3} = \frac{1}{2}
 \end{aligned}$$

$$\text{6b)} \quad \lim_{x \rightarrow 0} \sec 2x$$

$$\text{6c)} \quad \lim_{x \rightarrow 3} \tan\left(\frac{\pi x}{4}\right)$$

$$\text{6d)} \quad \lim_{x \rightarrow 2} \cot\left(\frac{3\pi}{2}x\right)$$

Use the graphs below to find the following limits(if they exist)



$$7a) \lim_{x \rightarrow 0} f(h(x))$$

$$= f(\lim_{x \rightarrow 0} (h(x)))$$

$$= f(0)$$

$$= -1$$

$$7b) \lim_{x \rightarrow 0} \left[ 2f(x) - \frac{h(x)}{f(x)} \right]$$

$$= \lim_{x \rightarrow 0} 2f(x) - \lim_{x \rightarrow 0} \frac{h(x)}{f(x)}$$

$$= 2 \lim_{x \rightarrow 0} f(x) - \frac{\lim_{x \rightarrow 0} h(x)}{\lim_{x \rightarrow 0} f(x)}$$

$$= 2 \cdot (-1) - \frac{0}{-1}$$

$$= -2$$

$$7c) \lim_{x \rightarrow 0} h(f(x))$$

$$7d) \lim_{x \rightarrow -1} f(x) \cdot 3h(x)$$

$$7e) \lim_{x \rightarrow 2} [f(2h(x)) + h(3f(x))]$$

## 8) AP MULTIPLE CHOICE EXAMPLES

1)  $\lim_{x \rightarrow \frac{\pi}{6}} \sec^2 x =$

(A)  $\frac{3}{4}$

(B)  $\frac{\sqrt{3}}{2}$

(C)  $\frac{4}{3}$

(D)  $\frac{2\sqrt{3}}{3}$

2) If  $f(x) = \begin{cases} x^2 + 3, & x \neq 1 \\ 1, & x = 1 \end{cases}$ , then  $\lim_{x \rightarrow 1} f(x) =$

(A) 1

(B) 2

(C) 3

(D) 4

3) Let  $f$  be a function given by  $f(x) = \begin{cases} 3 - x^2, & \text{if } x < 0 \\ 2 - x, & \text{if } 0 \leq x < 2 \\ \sqrt{x - 2}, & \text{if } x > 2 \end{cases}$ .

Which of the following statements are true about  $f$ ?

I.  $\lim_{x \rightarrow 0} f(x) = 2$

II.  $\lim_{x \rightarrow 2} f(x) = 0$

III.  $\lim_{x \rightarrow 1} f(x) = \lim_{x \rightarrow 6} f(x)$

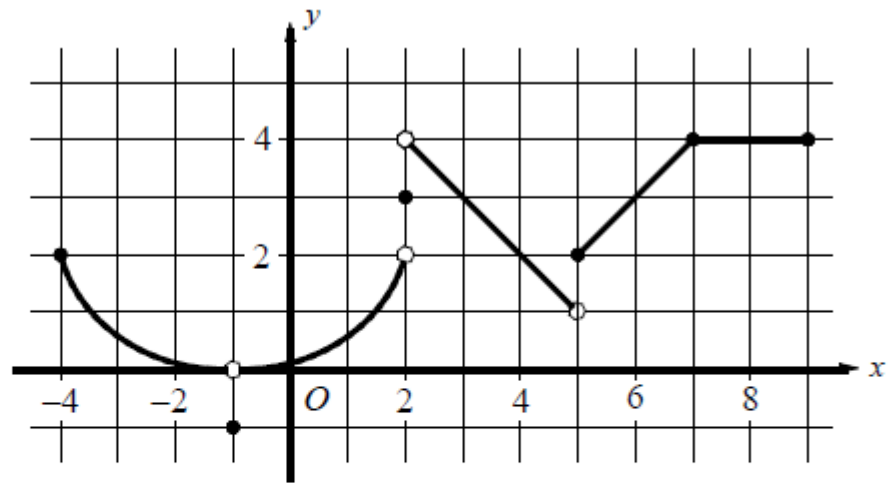
(A) I only

(B) II only

(C) II and III only

(D) I, II, and III

4)



The figure above shows the graph of  $y = f(x)$  on the closed interval  $[-4, 9]$ .

Find  $\lim_{x \rightarrow -1} \cos(f(x))$ .

(A) DNE

(B) 1

(C) 0

(D) -1

5)

$$\lim_{x \rightarrow 0} \frac{-x^2 + 4}{x^2 - 1} =$$

A) 1

B) 0

C) -4

D) -1

6)  $\lim_{x \rightarrow 0} \frac{\sqrt{4+x} - 2}{x} =$

(A)  $\frac{1}{8}$

(B)  $\frac{1}{4}$

(C)  $\frac{1}{2}$

(D) nonexistent

7)  $\lim_{x \rightarrow 3} \frac{\frac{1}{x} - \frac{1}{3}}{x - 3} =$

(A)  $-\frac{1}{9}$

(B)  $\frac{1}{9}$

(C)  $-9$

(D)  $9$