

Limits to Infinity

w-up: Give the equation of the horizontal asymptote(if any) for each function. If you do not remember how to find it, use the graphing calculator to help and/or verify your answer.

$$A) f(x) = \frac{3x+1}{x-1}$$

$$B) f(x) = -\frac{2}{x^2+1}$$

$$C) f(x) = \frac{2x^2-1}{x+4}$$

Finding Horizontal Asymptotes

Degree of Numerator = Degree of Denominator

$$y = \frac{\text{leading coefficient of numerator}}{\text{leading coefficient of denominator}}$$

Degree of Numerator < Degree of Denominator the H.A.

$$y = 0$$

Degree of Numerator > Degree of Denominator the H.A.

NO Horizontal Asymptote (but will have a slant/other asymptote)

Reminder: Horizontal Asymptotes are **NOT** values which make a function undefined and **CAN** contain points from the function.

Limit to infinity: The y-value a graph approaches as the x-values get infinitely large ($+\infty$) or infinitely small ($-\infty$).

Find the $\lim_{x \rightarrow \infty} f(x)$ for the above functions (A-C).

Find the $\lim_{x \rightarrow -\infty} f(x)$ for the above functions (A-C).

Use the graphing calculator to evaluate the following limit. $\lim_{x \rightarrow \infty} \frac{\sin x}{x}$

ZERO is the limit of any function containing a fraction where the denominator increases without bound but the numerator **DOES NOT**. NOTE: although zero is the limit, it is NOT a horizontal asymptote! We call this non-asymptotic behavior.

Special Case

EX1) $\lim_{x \rightarrow \infty} \sin x$

OSCILLATION

Infinite Limits when *Limits are taken to Infinity*(so, the limit DNE but can be denoted with $\pm\infty$)

EX2) $\lim_{x \rightarrow \infty} x^3 - 1,000,000,000,000x - 1,000,000,000,000$

HIGHEST POWER WINS!

EX3) $\lim_{x \rightarrow -\infty} \frac{3x^2 - 2x + 1}{x + 4}$

Determine the sign of infinity by dividing signs of numerator and denominator!

EX4) $\lim_{x \rightarrow \infty} \frac{3x - 2}{\sqrt{2x^2 + 1}}$

EX5) $\lim_{x \rightarrow -\infty} \frac{3x - 2}{\sqrt{2x^2 + 1}}$