

Other Methods of Integration

W-up: For each example, identify what you will let “u” equal and explain (but do not finish) how you would finish the integration.

$$\text{A) } \int \frac{5x}{5x^2-3} dx \quad \text{B) } \int \frac{3}{9x^2+4} dx \quad \text{C) } \int \frac{7x^2}{7x^2+4} dx \quad \text{D) } \int \frac{x+2}{\sqrt{16-9x^2}} dx$$

Other methods to try when integrating:

“Adding Zero” Adding and subtracting the same value or expression to help “u”-substitution work out.

$$\text{EX) } \int \frac{2x}{x^2+6x+10} dx$$

Since “u” = $x^2+6x+10$ would yield a $\frac{du}{dx} = 2x+6$

Rewrite the integral as $\int \frac{2x+6-6}{x^2+6x+10} dx$ or $\int \frac{2x+6}{x^2+6x+10} dx - \int \frac{6}{x^2+6x+10} dx$

and solve remaining integrals!

$$\text{EX) } \int \frac{1}{1+e^x} dx$$

Multiply numerator and denominator by the conjugate (when denominator contains a binomial with a trig. function)

EX) $\int \frac{1}{1+\sin x} dx$

EX) $\int \frac{1}{\sec x - 1} dx$

“THINK IDENTITIES”