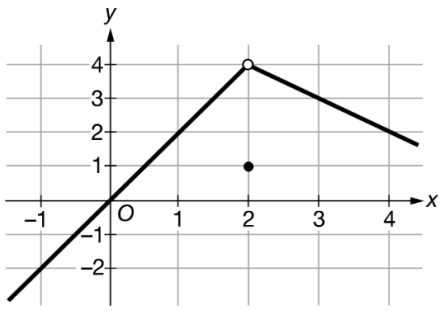
Unit 1 AP Classroom Practice for Sections 1-2

1)



Graph of f

What is the $\lim_{x \to 2} f(x)$?

(A) $\frac{1}{2}$

(B) 1

(C) 4

(D) The limit does not exist.

2) Of the following tables, which best reflects the values of a function g for which $\lim_{x \to 7} g(x) = 6$?

(A)

x	5.85	5.90	5.95	5.99	6.01	6.05	6.10	6.15
$g(x)$	7.126	7.075	7.033	7.006	6.995	6.977	6.964	6.960

(B)

x	6.85	6.90	6.95	6.99	7.01	7.05	7.10	7.15
$g(x)$	5.620	5.837	5.961	5.998	5.999	5.964	5.863	5.709

(C)

x	6.85	6.90	6.95	6.99	7.01	7.05	7.10	7.15
$g(x)$	5.919	5.942	5.969	5.993	7.017	7.087	7.177	7.269

(D)

x	6.85	6.90	6.95	6.99	7.01	7.05	7.10	7.15
$g(x)$	1.362	5.954	10.691	14.690	6.010	6.049	6.095	6.140

3) Let f be a function that is defined for all real numbers x. Of the following, which is the best interpretation of the statement $\lim_{x \to 3} f(x) = 5$?

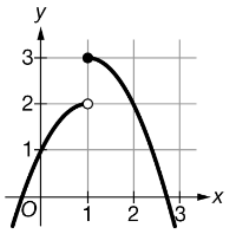
(A) The value of the function f at $x = 3$ is 5.

(B) The value of the function f at $x = 5$ is 3.

(C) As x approaches 3, the values of $f(x)$ approach 5.

(D) As x approaches 5, the values of $f(x)$ approach 3.

4)



Graph of *f*

The graph of a function f is shown above. Which of the following statements is true?

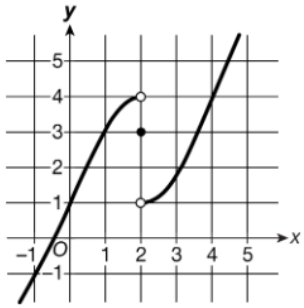
(A) $\lim_{x \to 1} f(x) = 2.5$

(B) $\lim_{x \to 1} f(x) = 3$

(C) $\lim_{x \to 1} f(x)$ does not exist because the left-hand and right-hand limits of $f(x)$ as x approaches 1 do not exist.

(D) $\lim_{x \to 1} f(x)$ does not exist because while the left-hand and right-hand limits of $f(x)$ as x approaches 1 exist, their values are not equal.

5)



Graph of *f*

The graph of the function f is shown above. What is $\lim_{x \to 2^+} f(x)$?

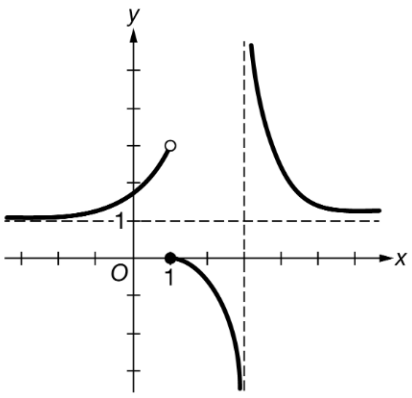
(A) 1

(B) 3

(C) 4

(D) nonexistent

6)



Graph of *f*

The graph of a function f is shown above. Which of the following statements is true?

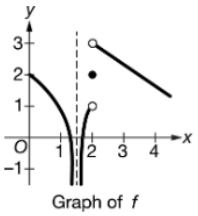
(A) $\lim_{x \to 1} f(x) = 1.5$

(B) $\lim_{x \to 1} f(x) = 0$

(C) $\lim_{x \to 1} f(x)$ does not exist because the left-hand and right-hand limits of $f(x)$ as x approaches 1 do not exist.

(D) $\lim_{x \to 1} f(x)$ does not exist because while the left-hand and right-hand limits of $f(x)$ as x approaches 1 exist, their values are not equal.

7)



Graph of f

The graph of the function f is shown above. What is $\lim_{x \to 2^+} f(x)$?

(A) 3

(B) 2

(C) 1

(D) nonexistent

8)

x	3.9	3.99	3.999	3.9999	4.0001	4.001	4.01	4.1
$f(x)$	5.8	5.85	5.9	5.95	6.999	6.99	6.9	6

The table above gives values of the function f at selected values of x. Which of the following conclusions is supported by the data in the table?

(A) $\lim_{x \to 4} f(x) = 6$

(B) $\lim_{x \to 4} f(x) = 7$

(C) $\lim_{x \to 4^-} f(x) = 6$ and $\lim_{x \to 4^+} f(x) = 7$

(D) $\lim_{x \to 4^-} f(x) = 7$ and $\lim_{x \to 4^+} f(x) = 6$

9)

$$f(x) = \begin{cases} 5x - 3 & \text{for } x < 2 \\ 9 & \text{for } x = 2 \\ 4x + 3 & \text{for } x > 2 \end{cases}$$

Let f be the piecewise function defined above. The value of $\lim_{x \to 2^+} f(x)$ is

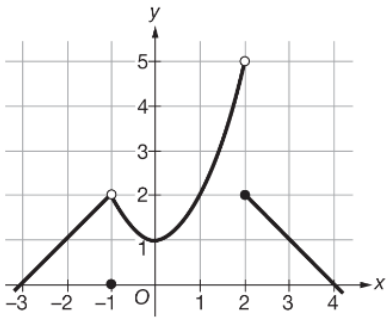
(A) 7

(B) 9

(C) 11

(D) nonexistent

10)



Graph of f

The graph of the function f is shown above. What is $\lim_{x \to -1} f(f(x))$?

(A) 1

(B) 2

(C) 5

(D) nonexistent

11)

$f(2) = 3$	$\lim_{x \to 2} f(x) = 4$
$g(2) = -6$	$\lim_{x \to 2} g(x) = -6$
$h(2) = -3$	$\lim_{x \to 2} h(x) = 2$

The table above gives selected values and limits of the functions f, g, and h. What is $\lim_{x \to 2} (h(x)(5f(x) + g(x)))$?

(A) -27

(B) -20

(C) 28

(D) 34

12) If f is the function defined by $f(x) = \frac{x^2-4}{x^2+x-6}$, then $\lim_{x \to 2} f(x)$ is

(A) 0

(B) $\frac{2}{3}$

(C) $\frac{4}{5}$

(D) nonexistent

13) If f is the function defined by $f(x) = \frac{x^2-4}{\sqrt{x}-\sqrt{2}}$, then $\lim_{x \to 2} f(x)$ is equivalent to which of the following?

(A) $\lim_{x \to 2} (x+2)\left(\sqrt{x}+\sqrt{2}\right)$

(B) $\lim_{x \to 2} \left(\sqrt{x}+\sqrt{2}\right)$

(C) $\lim_{x \to 2} \left(x\sqrt{x}-2\sqrt{2}\right)$

(D) $\lim_{x \to 2} (x+2)\left(x^2+4\right)$

14)

$$f(x) = \begin{cases} \frac{(x-1)^2(x+1)}{|x-1|} & \text{for } x \neq 1 \\ 2 & \text{for } x = 1 \end{cases}$$

If f is the function defined above, then $\lim_{x \to 1} f(x)$ is

(A) 0

(B) 1

(C) 2

(D) nonexistent

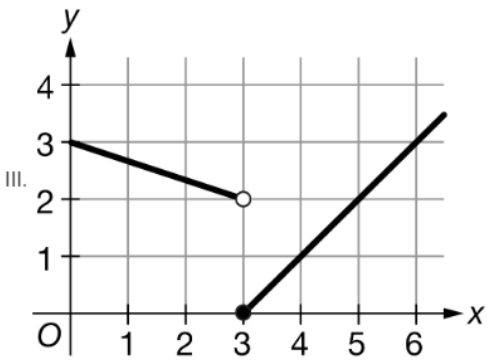
15) If h is a piecewise linear function such that $\lim_{x \to 3} h(x)$ does not exist, which of the following could be representative of the function h ?

I. $h(x) = \begin{cases} 12 - x & \text{for } x < 3 \\ 4x - 3 & \text{for } x > 3 \end{cases}$

II.

x	0	1	2	3	4	5	6
$h(x)$	3	$\frac{8}{3}$	$\frac{7}{3}$	0	1	2	3

III.



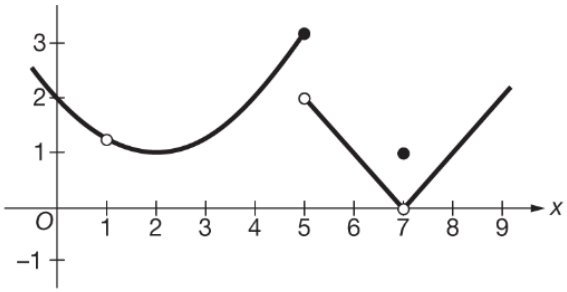
(A) I only

(B) II only

(C) III only

(D) II and III only

16)



Graph of f

The graph of the function f is shown above. What are all values of x for which f has a removable discontinuity?

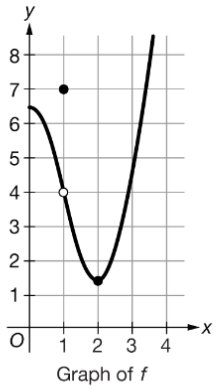
(A) 1 only

(B) 5 only

(C) 1 and 7 only

(D) 1, 5, and 7

17)



Graph of f

The graph of the function f is shown above. Which of the following could be a table of values for f?

(A)

x	0.95	0.99	1	1.001	1.05
$f(x)$	6.9025	6.9801	7	7.0020	7.1025

(B)

x	0.95	0.99	1	1.001	1.05
$f(x)$	4.1624	4.0325	7	3.9968	3.8376

(C)

x	0.95	0.99	1	1.001	1.05
$f(x)$	4.1624	4.0325	4	3.9968	3.8376

(D)

x	0.95	0.99	1	1.001	1.05
$f(x)$	4.1624	4.0325	undefined	3.9968	3.8376

18) Let f be the function defined by $f(x) = \frac{3x^3+2x^2}{x^2-x}$. Which of the following statements is true?

(A) f has a discontinuity due to a vertical asymptote at $x = 0$ and at $x = 1$.

(B) f has a removable discontinuity at $x = 0$ and a jump discontinuity at $x = 1$.

(C) f has a removable discontinuity at $x = 0$ and a discontinuity due to a vertical asymptote at $x = 1$.

(D) f is continuous at $x = 0$, and f has a discontinuity due to a vertical asymptote at $x = 1$.

19)

$$f(x) = \begin{cases} 2x+3 & \text{for } x < 1 \\ 5 & \text{for } x = 1 \\ -4x+9 & \text{for } 1 < x < 3 \\ 4 & \text{for } x = 3 \\ x-6 & \text{for } x > 3 \end{cases}$$

Let f be the piecewise function defined above. Which of the following statements is false?

(A) f is continuous at $x = 1$.

(B) f is continuous at $x = 2$.

(C) f is continuous at $x = 3$.

(D) f is continuous at $x = 4$.

20) Which of the following functions are continuous on the interval $0 < x < 5$?

I. $f(x) = \frac{x-3}{x^2-9}$

II. $g(x) = \frac{x-3}{x^2+9}$

III. $h(x) = \ln(x-3)$

(A) II only

(B) I and II only

(C) I and III only

(D) II and III only

21) Which of the following functions is not continuous on the interval $-\infty < x < \infty$?

(A) $f(x) = x^4 + x^3 + x^2 + x + 1$

(B) $g(x) = \frac{1}{x^3+x^2+x+1}$

(C) $h(x) = \frac{\pi}{2}\sin x$

(D) $k(x) = \frac{1}{1+e^{-x}}$

22)

$$f(x) = \begin{cases} x^2 + b^2 & \text{for } x < 2 \\ bx + 2b & \text{for } x \geq 2 \end{cases}$$

Let f be the function defined above, where b is a constant. For what values of b, if any, is f continuous at $x = 2$?

(A) 0 only

(B) 2 only

(C) 0 and 2

(D) There is no such b.

23) **CALCULATOR NEEDED**

$$f(x) = \begin{cases} \frac{\sin(3x)}{6x} & \text{for } x \neq 0 \\ c & \text{for } x = 0 \end{cases}$$

The function f is defined above, where c is a constant. For what value of c is f continuous at $x = 0$?

(A) 0

(B) $\frac{1}{2}$

(C) 1

(D) 2

24) **CALCULATOR NEEDED**

$$f(x) = \begin{cases} 2 - \sin x & \text{for } x \leq 1 \\ cx\sqrt{x^2 + 2} + c & \text{for } x > 1 \end{cases}$$

Let f be the function defined above, where c is a constant. For what value of c is f continuous for all x?

(A) 1.159

(B) 0.424

(C) 0.409

(D) There is no such value of c.

25)

$$f(x) = \begin{cases} \sin x & \text{for } x < 0 \\ \cos x & \text{for } 0 \leq x \leq \frac{3\pi}{2} \\ \tan x & \text{for } \frac{3\pi}{2} < x \leq 2\pi \\ \cot x & \text{for } 2\pi < x \leq \frac{5\pi}{2} \end{cases}$$

Let f be the function given above. On which of the following intervals is f continuous?

(A) $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$

(B) $\left(\frac{\pi}{4}, \pi\right)$

(C) $\left(\pi, \frac{7\pi}{4}\right)$

(D) $\left(\frac{7\pi}{4}, \frac{5\pi}{2}\right)$